

Write a short note on the following

i) The following sequence of operation is performed on a stack:

push(1) , push(2) ,pop , push(1) ,push(2), pop ,pop,pop,push(2),pop

determine the sequences of popped out values.

Solution- let assume the sequence (2,2,1,1,2) fill into stack.

Pop sequence can be like this

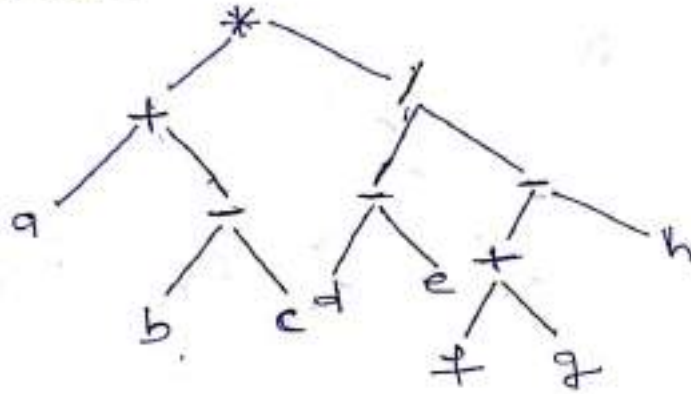
Operation	stack	pop sequence
Push 1	1	
Push 2	1,2	
Pop	1	2
Push 1	1,1	
Push 2	1,1,2	
Pop	1,1	2,2
Pop	1	2,2,1
Pop	Empty	2,2,1,1
Push 2	2	
Pop	Empty	2,2,1,1,2

ii) Write the preorder expression of the following algebraic expression

$$[a+(b-c)]*[(d-e)/(f+g-h)]$$

Answer-

→ Convert given algebraic equation into Binary Tree



Preorder :- Root, Left, Right

Preorder of given tree
*, +, a, -, b, c, /, -, d, e, +, f, g, h

iii) Arrange the following complexity function in increasing order.

$O(n^2)$, $O(n^3)$, $O(n \log n)$, $O(2^n)$, $O(\log n)$, $O(1)$, $O(n^4)$, $O(3^n)$, $O(\sqrt{n})$, $O(n^n)$

Answer- $O(1) < O(\log n) < O(\sqrt{n}) < O(n \log n) < O(n^2) < O(n^3) < O(n^4) < O(2^n) < O(3^n) < O(n^n)$

iv) What is the run time complexity of quick sort when the list is already sorted.

Answer- $O(n \log n)$ [it also depend on pivot selection]

v) What is garbage collection .

answer- Garbage collection is the systematic recovery of pooled computer storage that is being used by a program when that program no longer needs the storage. ... Garbage collection is an automatic memory management feature in many modern programming languages, such as Java and languages in the .NET framework.

How we can reduce the no of bits while representing the data which will result in saving of space while storing data and saving transmission time. conclude your answer by solving the mention string.

String: a a b a a c d a a b b b d e a a a a b b d d c c c d c a a b b c a a b b a a b b a a

How many bits we required by using 8 bit ASCII Code , by using own code , and by using huffman,s algorithm.

Answer.

Huffman coding (3)

→ This is used for data compression. It means using Huffman's code we can reduce no. of bits representing the data, which will result in saving of space while storing data and saving transmission time and bandwidth in data transmission.

→ Huffman's coding we get a variable length code.

Example

a a b a a c d a a b b b d e a a a a b b d d c c c d c a a b b c a a b b a a b b a a

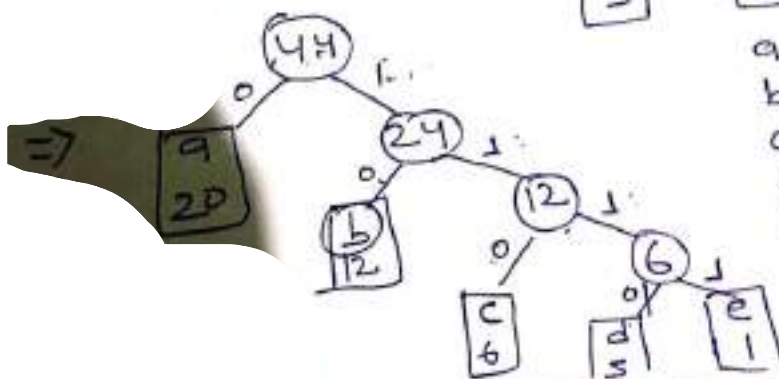
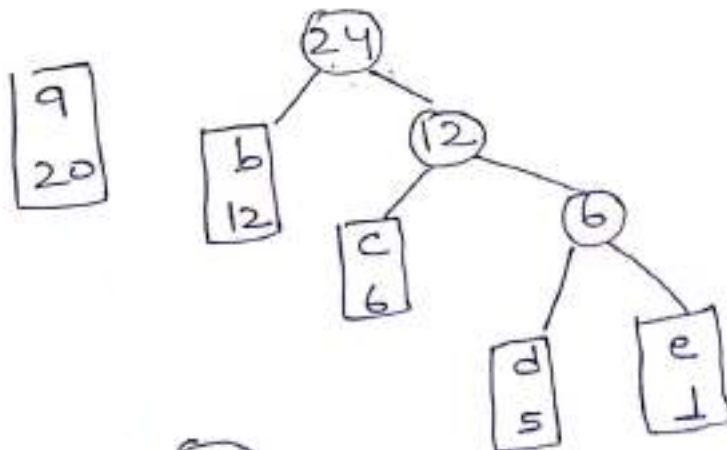
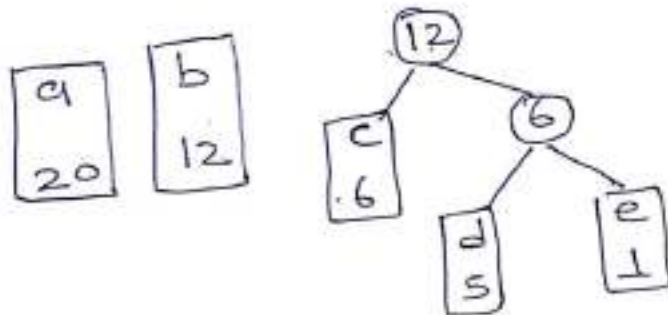
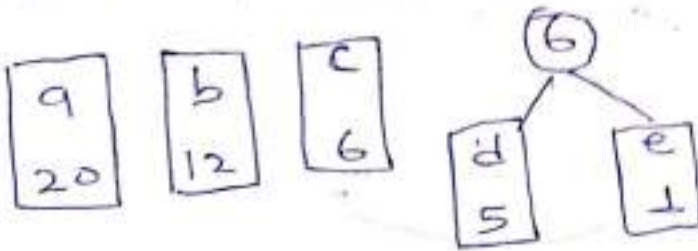
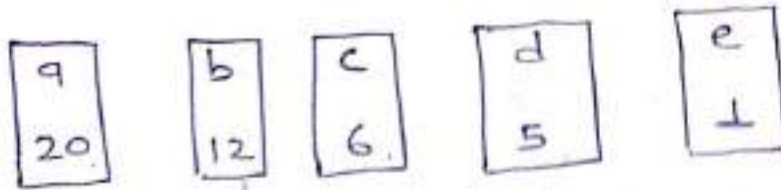
char	frequency	No. of bits using 8 bit ASCII code
a	20	$20 * 8 = 160$
b	12	$12 * 8 = 96$
c	6	$6 * 8 = 48$ ✓
d	5	$5 * 8 = 40$
e	1	$1 * 8 = 8$
Total		352 bits ✓

★ As in above text has only 5 character so we can make our own 5 bit code as shown below

a - 000
 b - 010
 c - 011
 d - 100
 e - 101

if we do so then total no. of bits require is equal to $44 * 3 = 132$ bits

★ Now Let us make a Huffman tree by considering frequency of characters in given text



a	1	0		1 * 20		
b	1	1	0	2 * 12		
c	1	1	1	0	3 * 6	
d	1	1	1	1	0	4 * 5
e	1	1	1	1	1	1 * 1
				86		

$$1 * 20 + 2 * 12 + 3 * 6 + 4 * 5 + 4 * 1 = \underline{86}$$

No. of bit required

using 8 bit ASCII code = 352
using our own code = 132
using Huffman's algo = 86

Suppose we have an array of numbers $a[1], \dots, a[n]$ in which the first i number $a[1], \dots, a[i]$ has been sorted into ascending order, and remaining numbers $a[i+1], \dots, a[n]$ has been in descending order. The aim is to sort the entire array in ascending order, design an algorithm which merges the two sorted lists into a second array $b[1], \dots, b[n]$ and copies the result back into a . show that the algorithm takes time $O(n)$.

Answer.

```

★ Merge procedure
Merge (A, B, q, r)
{
  n1 = q - p + 1
  n2 = r - q
  Let L[1.....n1+1] and R[1 to n2+1] be new arrays.
  for (i = 1 to n1)
    L[i] = A[p+i-1]
  for (j = 1 to n2)
    R[j] = A[r+1-j]
  L[n1+1] = ∞
  R[n2+1] = ∞
  i = 1, j = 1
  for (k = p to r)
    if (L[i] ≤ R[j])
      A[k] = L[i]
      i = i + 1
    else A[k] = R[j]
      j = j + 1
}

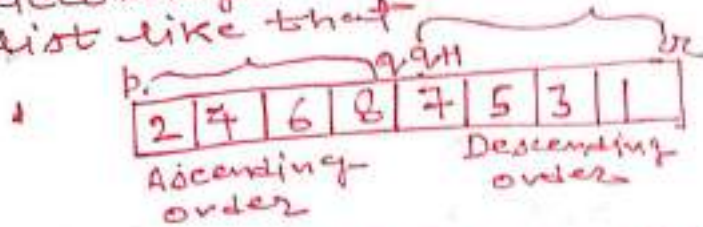
★ Merge sort procedure
Merge sort (A, p, r)
{
  if (p < r)
  {
    q = ⌊(p+r)/2⌋
    merge sort (A, p, q)
    merge sort (A, q+1, r)
    merge (A, p, q, r)
  }
}

```

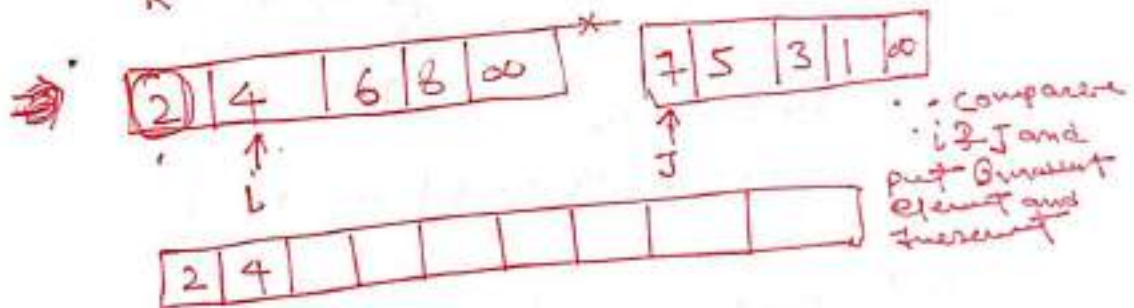
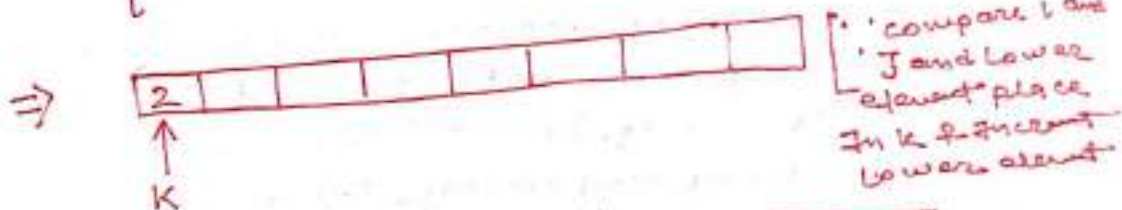
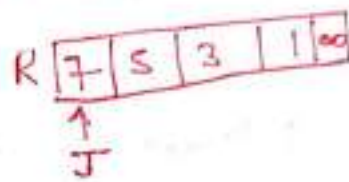
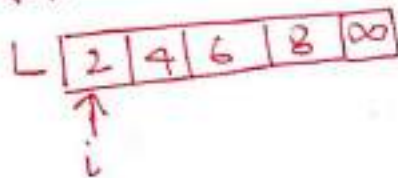
→ ~~Stop~~ Stop

→ Let's understand by Example.

According to the question, we have two list like that



According to the merge algorithm we take two list



follow this process until you find the entire sorted array

★ Second way to complete the question.

1- one given array is already sorted.

2- Second array is in descending order.
So apply merge in second array
and make it in ascending order.

3- Apply merge in both arrays which
are already sorted individually.
& compare till last element is not
sorted.

★ Total time complexity

In given arrays we are compare two
list. In given list total NO. of
elements are n . So we have to do
 n comparison and every time we
compare the list ($i \neq j$) and written
into new array means n elements copied
into new array.

$$\text{So we have } (n+n) = O(n)$$

Total time complexity require
 $= O(n)$

Design a data representation which sequentially map n data objects into an array $a[1,n]$, n_1 of these data objects are stacks and remaining n_2 equal to $n-n_1$ are queues. Write algorithm to add and delete elements from these objects.

★ Insertion of elements in stack using array

```
int Stack[max]
int TOP = -1
void push (int item)
{
    if (TOP == max-1)
        printf ("overflow");
    else
    {
        TOP = TOP + 1;
        Stack[TOP] = item;
    }
    return;
}
```

★ Deletion of element in stack using array

```
int pop ( )
{
    int temp;
    if (TOP == -1)
    {
        printf ("underflow");
        return -1;
    }
    else
    {
        return temp = Stack[TOP];
        TOP = TOP - 1;
    }
    return temp;
}
```

★ Insertion of element in Queue.

QInsert(Queue, N2, front, Rear, Item)

1- (Queue already filled?)

if front = 1 and Rear = N2 or if front = Rear + 1
then write overflow & return.

2- (Find New value of Rear)

if front = Null then (Queue initially empty)

Set front = 1 and Rear = 1

else if Rear = N2 then Set Rear = 1

else

Rear = Rear + 1

3- Set Queue[Rear] = Item

4- Return.

★ Deletion of elements in Queue.

1- (Queue already empty)

if front = Null then

write underflow and return;

2- Set Item = Queue[front]

3- (Find New value of front)

if front = Rear then

Set front = Null and Rear = Null

else

if front = N then

Set front = 1

else

Set front = front + 1

4- Return.